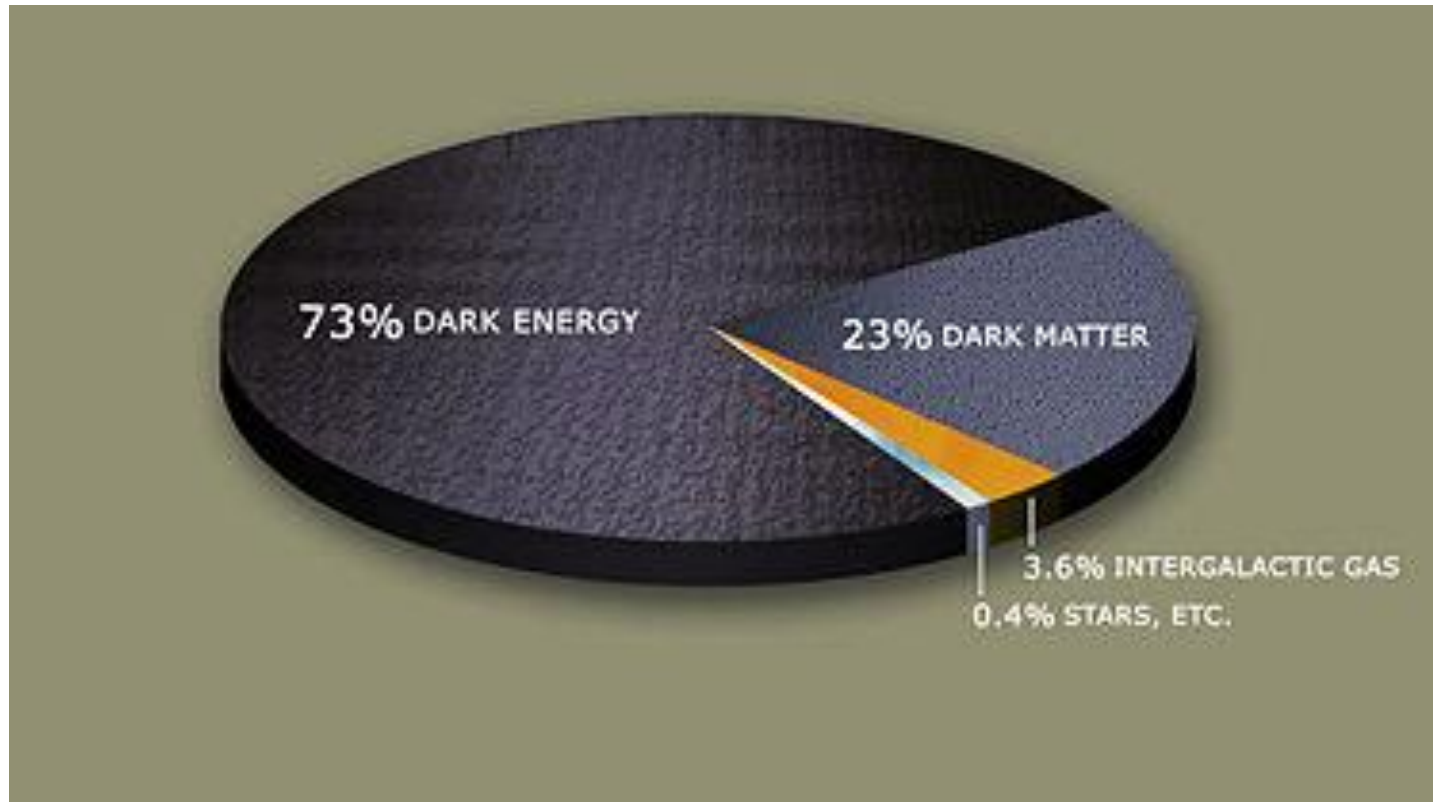


# Neutralino dark matter stars can not exist

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# The portion of the universe



# The structure

- Standard model particles:  
super-cluster → cluster → Galaxy → star

- Dark matter: (neutralino?)

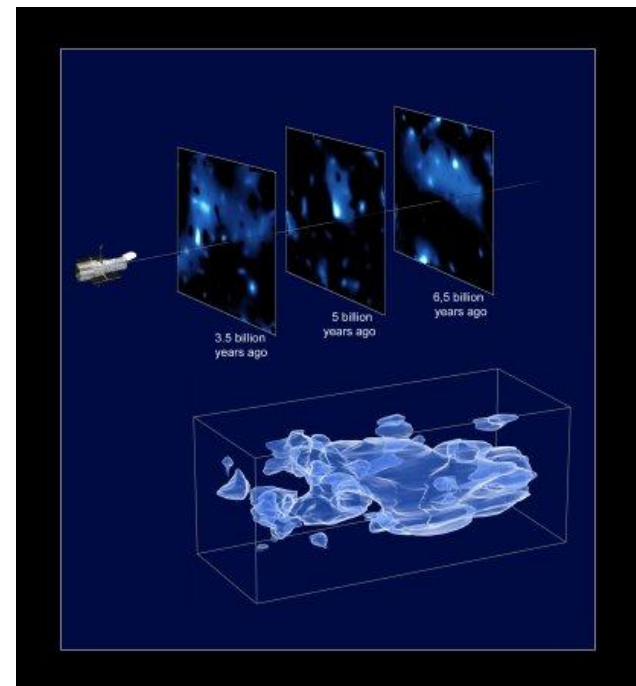
R. Massey *et al.*, *Nature* **445** (2007) 286

gravitational seed

→ dark galaxy ?

→ pure dark matter star?

Not the dark star in “D. Spolyar, K. Freese and P. Gondolo, *Phys. Rev. Lett.* **100**, 051101 (2008)”.



Date: 08 Jan 2007

Satellite: Hubble Space Telescope

Depicts: COSMOS dark matter survey

# SUSY dark matter

- Neutralino:
  - R-parity: stable
  - heavy: several 100 GeV
  - weak interaction: hard to detect
  - Majorana fermion: self-annihilation

# condition to create a star

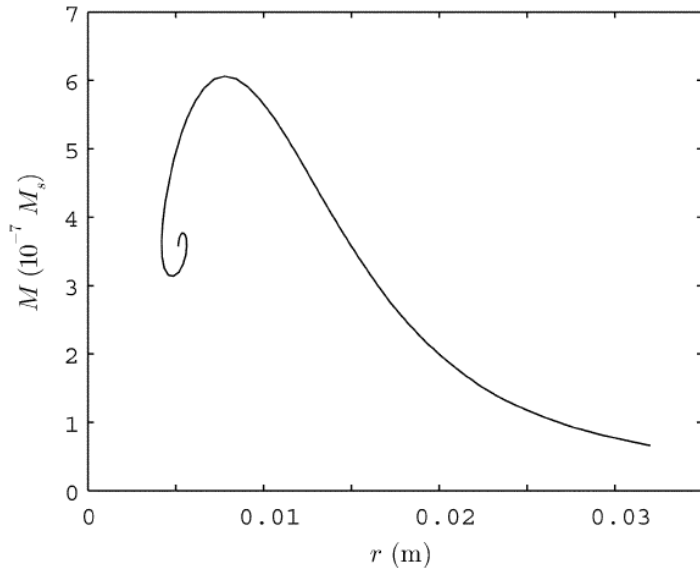
- Pressure : to avoid collapse
- Finite volume
- Can neutralino satisfy these condition?

Fermion: Pauli exclusive force

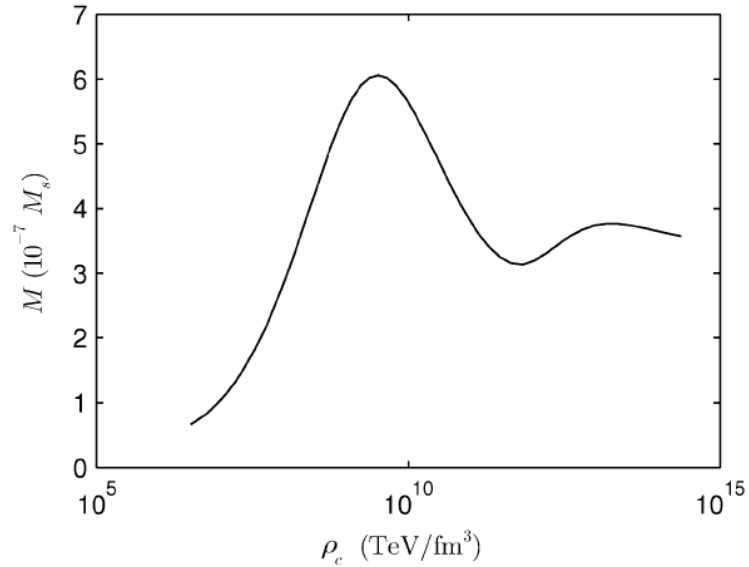
example : neutron star, quark star

stable : R-parity

# Turn out



**Fig. 2** The mass-radius relation of the neutralino star.  $M_S$  denotes the mass of the sun.



**Fig. 3** The mass of the neutralino star as a function of its central mass density.  $M_S$  denotes the mass of the sun.

$$\frac{dp}{dr} = -\frac{GM\rho}{r^2} \left(1 + \frac{p}{\rho}\right) \left(1 + \frac{4\pi r^3 p}{M}\right) \left(1 - \frac{2GM}{r}\right)^{-1}$$

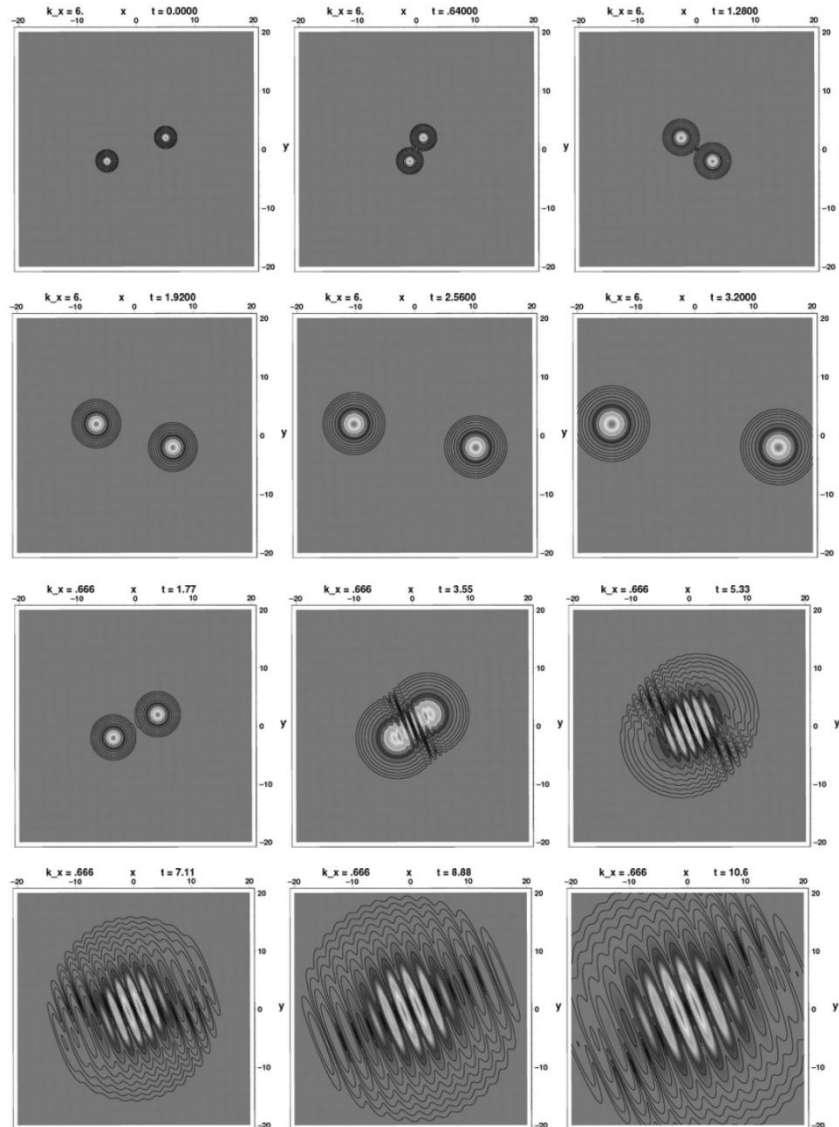
where

$$M(r) = \int_0^r 4\pi r'^2 \rho(r') dr'$$

$$p = \frac{1}{3\pi^2} \int_0^{k_F} \frac{k^4 dk}{\sqrt{k^2 + m^2}} - \frac{1}{2} m_H^2 H^2 - \frac{1}{2} m_h^2 h^2 + \frac{1}{2} m_Z^2 Z^2.$$

Question: If the interaction between neutralinos is weak, how can they exchange energy and become thermal

# Entanglement?



D. Pfenniger and V. M. G. Observatory,  
A&A 456, 45 (2006)

$$\sigma \sim \pi \lambda_{\text{dB}}^2$$

# The neutralino

$$Z_N^T \begin{pmatrix} M_1 & 0 & \frac{-ev_1}{2c_W} & \frac{ev_2}{2c_W} \\ 0 & M_2 & \frac{ev_1}{2s_W} & \frac{-ev_2}{2s_W} \\ \frac{-ev_1}{2c_W} & \frac{ev_1}{2s_W} & 0 & -\mu \\ \frac{ev_2}{2c_W} & \frac{-ev_2}{2s_W} & -\mu & 0 \end{pmatrix} Z_N$$

$$= \text{diag} \left( M_{\chi_1^0}, M_{\chi_2^0}, M_{\chi_3^0}, M_{\chi_4^0} \right)$$

$$\lambda_B = iZ_N^{1i} \kappa_i^0, \quad \lambda_A^3 = iZ_N^{2i} \kappa_i^0,$$

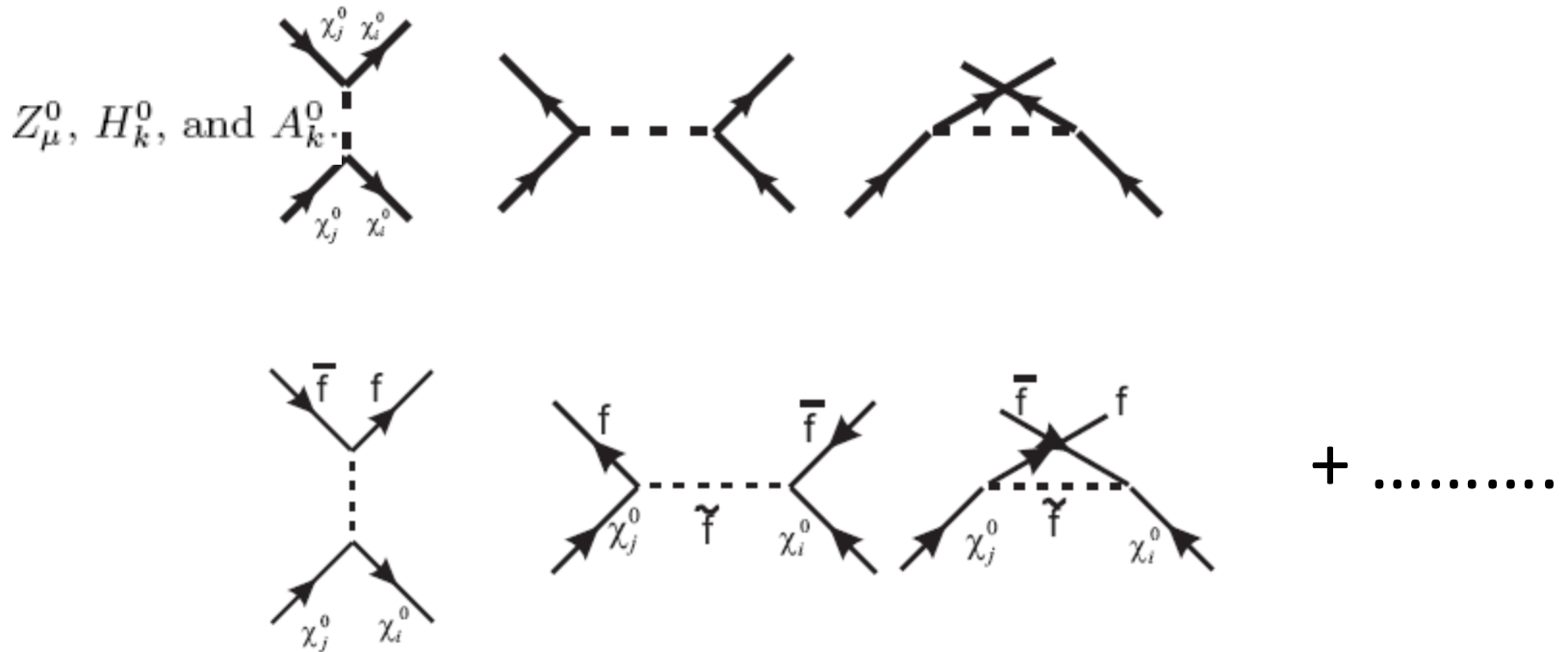
$$\Psi_{H_1}^1 = iZ_N^{3i} \kappa_i^0, \quad \Psi_{H_2}^2 = iZ_N^{4i} \kappa_i^0, \quad \chi_i^0 = \begin{pmatrix} \kappa_i^0 \\ \bar{\kappa}_i^0 \end{pmatrix}$$

$$M_{\chi_1^0} < M_{\chi_2^0} < M_{\chi_3^0} < M_{\chi_4^0}.$$



# Cross section

$$\frac{d\sigma}{d\Omega} = \frac{|P_1|}{16\pi^2 E_A E_B |v_A - v_B| E_{cm}} |M(P_A, P_B \rightarrow P_1, P_2)|^2$$



# Amplitude for s-channel

Elastic collision

$$M_{el Z_\mu^0}^{(s)} \sim \left(\frac{e}{s_W c_W}\right)^2 \bar{\chi}_1^0 \gamma^\mu \chi_1^0 \frac{1}{s - m_Z^2} \bar{\chi}_1^0 \gamma_\mu \chi_1^0$$

$$M_{el H_k^0, A_k^0}^{(s)} \sim \left(\frac{e}{s_W c_W}\right)^2 \bar{\chi}_1^0 \chi_1^0 \frac{1}{s - m_H^2} \bar{\chi}_1^0 \chi_1^0$$

annihilation

$$M_{ann Z_\mu^0}^{(s)} \sim \left(\frac{e}{s_W c_W}\right)^2 \bar{f} \gamma_\mu f \frac{1}{s - m_Z^2} \bar{\chi}_1^0 \gamma_\mu \chi_1^0$$

$$M_{ann H_k^0, A_k^0}^{(s)} \sim \left(\frac{e}{s_W c_W}\right) \bar{f}^c f Y_f \frac{1}{s - m_H^2} \bar{\chi}_1^0 \chi_1^0$$

Ignore portion , P<sub>L</sub> and P<sub>R</sub>

# Amplitude for t,u-channel

Elastic collision

$$M_{el H_k^0, A_k^0}^{(t,u)} \sim \left(\frac{e}{s_W c_W}\right)^2 \bar{\chi}_1^0 \chi_1^0 \frac{1}{tu - m_H^2} \bar{\chi}_1^0 \chi_1^0$$
$$M_{el Z_\mu^0}^{(t,u)} \sim \left(\frac{e}{s_W c_W}\right)^2 \bar{\chi}_1^0 \gamma^\mu \chi_1^0 \frac{1}{tu - m_Z^2} \bar{\chi}_1^0 \gamma_\mu \chi_1^0$$

annihilation

$$M_{ann}^{(t,u)} \sim \left(\frac{e}{s_W c_W}\right)^2 \bar{f}^c \chi_1^0 \frac{1}{tu - m_f^2} \bar{f} \chi_1^0$$

# conclusion

- Neutralinos follow collisionless Boltzmann equation
- Neutralino type of dark matter does not become a thermal star.